# Structural, Energetic, and Vibrational Properties of NO<sub>x</sub> Adsorption on Ag<sub>n</sub>, n = 1-8

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The density functional theory is used to explore structural, electronic, and vibrational properties of NO, NO<sub>2</sub>, and NO<sub>3</sub> adsorption on small silver clusters, Ag<sub>n</sub>, with n = 1-8. Generally, NO adsorbs in atop configuration, whereas NO<sub>2</sub> and NO<sub>3</sub> are adsorbed in bridge configuration. NO<sub>2</sub> and NO<sub>3</sub> introduce pronounced structural relaxations in the clusters. In particular, the transition size from planar to three-dimensional structures is modified. For each cluster size, the adsorption energies follow the trend  $E_a$  (NO)  $\leq E_a$  (NO<sub>2</sub>)  $\leq E_a$  (NO<sub>3</sub>). The adsorption energies show a marked odd/even alternation with a stronger bonding to odd clusters. Analysis of the electronic structure reveals an ionic bond mechanism for NO<sub>2</sub> and NO<sub>3</sub>. Odd/even effects are also present in vibrational properties of the adsorbed radicals. With respect to the gas phase, the largest shifts are calculated for adsorption on odd clusters. Possible implications of the results for Ag/Al<sub>2</sub>O<sub>3</sub> HC-SCR catalysts are discussed.

### I. Introduction

One of the main motivations for the study of gas phase atomic clusters is the possibility of novel chemical properties. Indeed, the pioneering experiments of cluster reactivity uncovered marked size variations.<sup>1–3</sup> For example, the reaction rate constants of H<sub>2</sub> with Fe<sub>n</sub> was measured to change several orders of magnitude in the size range Fe<sub>6</sub> to Fe<sub>68</sub>.<sup>2</sup> The observed changes were non-monotonic, and pronounced differences were observed from one cluster size to another. Because adsorption processes are influenced by both structural and electronic factors, the underlying reason for the size variations is a challenging issue. In the case of H<sub>2</sub> reactivity with Fe<sub>n</sub>, the reactivity strongly correlates with the cluster ionization thresholds.<sup>3</sup> Clusters with a low ionization threshold were measured to react more efficiently with H<sub>2</sub> than clusters with a high threshold.

Following the early experiments,<sup>1–3</sup> cluster reactivity in the gas phase has been explored for several transition metals and reactions.<sup>4</sup> Moreover, it has been possible to investigate the size dependence of catalytic reactions such as CO and H<sub>2</sub> oxidation on Pt<sub>n</sub>.<sup>5,6</sup> Clusters from the coinage metal group (Cu, Ag, and Au) have received special attention. The interest arises as these clusters show a regular and marked size variation in electronic properties, including ionization potentials and electronic affinities.<sup>7</sup> In addition to variations that correlate with electronic shell closings for delocalized electrons in an external potential,<sup>8</sup> this type of clusters exhibit odd/even alternations with respect to the number of atoms in the cluster.<sup>7,9</sup> Interestingly, similar size variations have been observed for chemical processes, such as O<sub>2</sub> reactivity and CO oxidation.<sup>10</sup>

In view of the large size-to-size variation in the reactivity of coinage metal clusters, it is intriguing that the active metal phase in the HC-SCR (selective catalytic reaction with hydro-carbons as the reducing agent) reaction of NO<sub>x</sub> over an Ag/Al<sub>2</sub>O<sub>3</sub> catalyst<sup>11</sup> has recently been proposed to be small Ag<sub>n</sub> clusters.<sup>12,13</sup> By comparing UV–vis spectra for an Ag/Al<sub>2</sub>O<sub>3</sub> catalyst with reference samples with known Ag<sub>n</sub> sizes, it was concluded

that the active clusters consist of less than eight atoms.<sup>12</sup> Moreover, *in situ* EXAFS (extended X-ray absorption fine structure spectroscopy) measurements revealed an average Ag–Ag coordination number of ~2.7, which suggests clusters as small as trimers or tetramers.<sup>13</sup> Of course, because the clusters are small, it is probable that the support material ( $\gamma$ -alumina) influences the catalytic properties of the metal clusters. The complexity of adsorption on multicomponent systems have recently been demonstrated for molecular adsorption on metals supported on oxides (see, for example, refs 14–16) and oxides supported on metals.<sup>17</sup>

Owing to the interesting intrinsic properties of  $Ag_n$  clusters and in an attempt to increase the understanding of the metal phase in the HC-SCR  $Ag/Al_2O_3$  catalyst for  $NO_x$  reduction, we have performed a systematic density functional theory (DFT)based study of  $NO_x$  adsorption on gas-phase  $Ag_n$  clusters with  $n \le 8$ . The sequence from NO to  $NO_3$  was considered, and results are presented for structural and energetic as well as vibrational properties.

The adsorption of NO on transition metal clusters has previously been explored within DFT for  $Pd_1-Pd_6$ ,<sup>18</sup> Fe<sub>1</sub>-Fe<sub>6</sub>,<sup>19</sup> Rh<sub>6</sub><sup>20</sup> and Cu<sub>4</sub>, Ag<sub>4</sub>, and Cu<sub>2</sub>Ag<sub>2</sub>.<sup>21</sup> These studies show that molecular NO is adsorbed preferably with N attached to the cluster. Moreover, NO is predicted to dissociate on Fe clusters larger than the monomer<sup>19</sup> and on Rh<sub>6</sub>.<sup>20</sup>

#### **II.** Computational Methods

DFT<sup>22,23</sup> is applied with the gradient corrected exchange correlation functional according to Perdew, Burke, and Ernzerhof (PBE).<sup>24</sup> The one-electron Kohn–Sham orbitals are expanded in a localized numerical basis set.<sup>25–27</sup> A double numerical basis set is used together with polarization functions. A real space cutoff of 4.5 Å is used for the basis functions. A pseudo potential<sup>28</sup> is utilized for Ag to describe the interaction between the valence electrons (4s <sup>2</sup>4p<sup>6</sup>4d<sup>10</sup>5s<sup>1</sup>) and the nucleus, together with the inner shell electrons. The Kohn–Sham equations are solved self-consistently using an integration technique based on weighted overlapping spheres centered at

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each atom. The direct Coulomb potential is obtained by projection of the charge density onto angular dependent weighting functions also centered at each atom. The Poisson equation is, thereafter, solved by one-dimensional integration.

The potential energy surfaces of the bare clusters and clusters with adsorbates are investigated by geometrical relaxation (without symmetry constraints) starting from several different configurations. For bare clusters larger than the tetramer, at least six different isomers were considered. All different atop and bridge sites were investigated for NO, NO<sub>2</sub>, and NO<sub>3</sub> adsorption on relevant neutral and cationic cluster isomers. That the reported structures are minima are confirmed by calculations of the vibrational spectra. The vibrational analysis is performed via numerical derivatives.

As a reference, Ag in the bulk phase is considered. These calculations apply periodic boundary conditions, and reciprocal space integration over the Brillouin zone is approximated with a finite sampling using the Monkhorst–Pack scheme.<sup>29,30</sup>

#### **III. Results and Discussion**

Bare neutral and charged silver clusters in the size range discussed here have been the subject of numerous first principles investigations.<sup>31–39</sup> These studies have established the relevant isomers and, particularly, the transition from two-dimensional (2D) to three-dimensional (3D) motifs. For neutral clusters, the transition occurs between hexamer and heptamer, whereas for cations, the first size with 3D structure is  $Ag_5^+$ . For the positively charge clusters, the early structural transition has been supported by ion mobility measurements.<sup>36</sup> Because Ag clusters follow the trend for clusters with one valence electron, they are less complex than the Au counterparts, which were shown to be 2D over a wider size range<sup>40,41</sup> owing to the delocalization of *d*-electrons.<sup>42</sup>

In this section, we start by presenting results for bare neutral and cationic clusters. Although these systems already have been thoroughly discussed in the literature, this provides an opportunity to evaluate the quality of the computational technique. Moreover, the properties of the bare clusters are essential to understand the results for  $NO_x$  adsorption. NO,  $NO_2$ , and  $NO_3$  adsorption will be discussed in the subsequent section.

**A. Bare Neutral and Cationic Clusters.** Results for bare and cationic cluster structures are presented in Figure 1, together with point group determination and energetic properties. For the neutral clusters, only the stable isomers are reported. Two isomers of  $Ag_8$  have similar stability. Instead of reviewing literature data of  $Ag_n$  isomers, we refer to the review in ref 35.

The spectroscopic constants of the dimer are calculated to 1.71 eV (binding energy), 2.61 Å (bond distance), and 179 cm<sup>-1</sup> (vibrational wavenumber). These results compare favorably with previous DFT reports using the same functional.<sup>40</sup> In ref 40, where a plane-wave pseudo potential method was used, the binding energy and bond distance were reported to be 1.62 eV and 2.63 Å, respectively. The corresponding experimental values are 1.66 eV,<sup>43</sup> 2.53 Å,<sup>44</sup> and 192 cm<sup>-1.43</sup>

The stable isomer of the trimer is the obtuse iso-scaled triangle. The angle is in this case  $75^{\circ}$ . The acute ( $55^{\circ}$ ) isomer is calculated to be 0.07 eV above the ground state. The structures for Ag<sub>4</sub> to Ag<sub>6</sub> are formed by decorating the triangle with one to three caps. These geometries are all planar. For the hexamer, the second best isomer (0.25 eV above the reported isomer) is a pentagonal pyramid, which is 3D. The stable heptamer is a pentagonal bi-pyramid. Thus, this structure is based on the second best geometry for Ag<sub>6</sub>. The ground state of the octamer



**Figure 1.** Structural models of low energy isomers of neutral (top) and cationic (bottom) clusters. The symmetry point group is indicated. For the neutral clusters, the cohesion energy is reported together with the monomer fragmentation energy (in parentheses). For  $Ag_n^+$  clusters with the same size, the relative ordering is reported. All energies are in eV.

is calculated to be a tetra-capped tetrahedron, which has  $T_d$  symmetry. This structure is preferred by 0.05 eV over the dodecahedron ( $D_{2d}$ ). The present results concerning relevant ground-state structures are in agreement with previous DFT reports.<sup>35,38</sup> The average bond distances for the ground-state clusters increase monotonically with cluster size and range from 2.61 Å for the dimer to 2.85 Å for the  $T_d$  isomer of Ag<sub>8</sub>. As expected, the bonds in these small clusters are contracted with respect to the nearest neighbor distance in the bulk, which in the present approach is calculated to be 2.99 Å. The experimental value is 2.89 Å.<sup>45</sup>

The cohesion energy of the clusters (Figure 1) is clearly reduced with respect to the bulk value, which is calculated to be 2.52 eV. The corresponding experimental value is 2.8 eV.<sup>45</sup> In agreement with previous reports,<sup>35,38</sup> the monomer fragmentation energy (Ag<sub>n</sub>  $\rightarrow$  Ag<sub>n-1</sub> + Ag) shows an odd/even alternation; even clusters are more stable than adjacent odd clusters.

The ground-state isomers for the cationic clusters are reported in the lower part of Figure 1. Upon ionization, the trimer becomes an equilateral triangle. The positively charged tetramer has the same ground-state structure as the neutral counterpart. For the pentamer, the stable isomer is 3D with  $D_2$  symmetry. Also for  $Ag_6^+$ , a change in structure as compared with the neutral case is predicted. The stable structure is a planar  $C_{2v}$ isomer. A 3D geometry with the same point symmetry group is 0.05 eV higher in energy. The  $D_{3h}$  isomer, which is the stable structure for the neutral hexamer, is 0.16 eV higher than the ground state. For the heptamer, a planar isomer with  $D_{6h}$ symmetry is calculated to be the stable structure. The pentagonal bi-pyramid, is a meta-stable configuration, which is 0.09 eV higher in energy. For  $Ag_8^+$ , the stable structure follows the pentagonal motif present for  $Ag_7^+$  and can be characterized as a pentagonal bi-pyramid with one cap. The bi-capped octahedron and dodecahedron are 0.05 and 0.07 eV, respectively, higher in energy. For the neutral octamer, the  $T_d$  isomer is competitive



**Figure 2.** Structural models of NO, NO<sub>2</sub>, and NO<sub>3</sub> adsorbed on Ag<sub>n</sub>. Two isomers (a and b) are reported for Ag<sub>7</sub>NO<sub>2</sub> and Ag<sub>6</sub>NO<sub>3</sub>, respectively. The corresponding adsorption energies with respect to ground state Ag<sub>n</sub> structures and the gas-phase adsorbates are reported in eV. Atomic color code: silver (blue metal), nitrogen (blue), and oxygen (red).

in energy. However, as a cation this isomer is calculated to be meta-stable by 0.46 eV.

From the stable neutral and cationic clusters, the adiabatic ionization potentials (AIP) have been evaluated. These are in eV: 7.78, 5.77, 6.46, 5.89, 6.73, 5.57, and 6.22 for  $Ag_2$  to  $Ag_3$ , respectively. Thus, there is marked odd/even alternation also in this electronic property.

**B.** NO<sub>x</sub> Adsorption on Ag<sub>n</sub>. We turn now to the issue of NO<sub>x</sub> adsorption on Ag<sub>n</sub>. First, the geometrical structures are presented together with the size evolution of the adsorption energies. Thereafter, the electronic structure is analyzed in some detail, and finally, the results are presented for vibrational properties.

1. Structural and Energetic Properties. At the top of Figure 2, the stable structures for  $Ag_nNO$  are reported. The cluster size dependence of the adsorption energy is shown in Figure 3.

Generally, NO prefers adsorption in an atop configuration. In this geometry, the Ag<sub>n</sub>-NO and N-O distances are about 2.17 and 1.18 Å, respectively. The Ag-N-O angle is ~130°. For the gas-phase NO, the N-O distance is calculated to be 1.15 Å. The HOMO<sup>46</sup> level of NO is the antibonding  $2\pi^*$  state. As NO is adsorbed,  $2\pi^*$  gets slightly occupied, which rationalizes the elongation of the NO distance as well as the bent adsorption structure. The difference between the singlet and triplet states for the odd Ag<sub>n</sub>NO systems is fairly small (within 0.2 eV). AgNO and Ag<sub>7</sub>NO are calculated to be singlets,



Figure 3. Adsorption energies of NO, NO<sub>2</sub>, and NO<sub>3</sub> on Ag<sub>n</sub>.

whereas the triplet state is preferred for Ag<sub>3</sub>NO and Ag<sub>5</sub>NO. The similar stability of the two spin states is most likely related to the low electronic affinity of NO.

Regarding the adsorption site,  $Ag_5NO$  is an exception. For this cluster size, NO is adsorbed in a bridge configuration with Ag-N and N-O distances of 2.27 and 1.21 Å, respectively. The underlying reason for the bridge preference on  $Ag_5$  is the electronic structure of the bare cluster. In this case, the HOMO level is a bonding orbital between the two Ag atoms connected to NO. This orbital interacts efficiently with the singly occupied  $2\pi^*$  of NO. The long N-O distance is a signature of this interaction.

The calculations do not predict any marked structural relaxations of Ag<sub>n</sub> upon NO adsorption. In all cases, the lowenergy structures of Ag<sub>n</sub> NO are related to the ground-state isomers of Ag<sub>n</sub>. However, in the case of Ag<sub>8</sub>NO, the preference between the dodecahedron  $(D_{2d})$  and the tetra-capped tetrahedron  $(T_d)$  is reversed. With NO adsorbed, the  $D_{2d}$  isomer is preferred by 0.05 eV over  $T_d$ . The minor structural relaxations signal a weak interaction, which also is calculated. With a clear odd/ even alternation, the adsorption energy is predicted to be in the range between 0.5 and 1 eV (Figure 3).

Adsorption of NO on Ag<sub>4</sub> has previously been studied using DFT in an implementation based on local basis functions and effective core potentials.<sup>21</sup> The adsorption energy was reported to be 0.89 eV and the N-O distance to be 1.16 Å for the same configuration as the one in Figure 2. This is in very good agreement with the present results of 0.90 eV and 1.17 Å, respectively.

We now consider NO<sub>2</sub> adsorption. With the exception of the monomer and dimer, NO2 prefers adsorption in a bridge configuration with an Ag–O distance of  $\sim 2.3$  Å. For NO<sub>2</sub>, the N-O distance is elongated upon adsorption. In the gas-phase, the calculated N–O distance is 1.20 Å. For  $Ag_nNO_2$ , the corresponding distance is  $\sim 1.25$  Å. Also the O–N–O angle is changed from 134° for the free molecule to  ${\sim}120^\circ$  when  $NO_2$ is adsorbed. In fact, the molecular structure of adsorbed NO<sub>2</sub> is close to what is calculated for the gas-phase nitrite, namely, an N–O distance of 1.28 Å and an O–N–O angle of 115°. Thus, the structural changes signal a bond mechanism with charge transfer from the cluster to NO2. This conclusion is, furthermore, supported by the cluster relaxations. For Ag<sub>2</sub>-Ag<sub>5</sub>, the metal structure of  $Ag_n NO_2$  is similar to that of the bare cluster case. However, in the range Ag<sub>6</sub>-Ag<sub>8</sub>, the clusters adopt structures that are relevant for the  $Ag_n$  cations, indicative of a cluster-toadsorbate charge transfer. For Ag<sub>6</sub>, NO<sub>2</sub> drives the transformation from the planar  $D_{3h}$  isomer to the 3D  $C_{2v}$ . The planar structure with the lowest energy (0.06 eV above the ground state) is for Ag<sub>6</sub>NO<sub>2</sub> based on the cationic ground state with  $C_{2v}$  symmetry (Figure 1). Regarding the 2D versus 3D preference, NO<sub>2</sub> has the opposite effect on Ag<sub>7</sub>, namely, that 2D

isomers are stabilized. In this case, the planar  $D_{6h}$  isomer is only 0.02 eV less preferred than the ground-state pentagonal bi-pyramid. Also for Ag<sub>8</sub>NO<sub>2</sub>, the ground-state structure is based on the cationic cluster structure, which is a capped pentagonal bi-pyramid. Low-energy structures based on relevant neutral cluster structures are at least ~0.1 eV above the ground state.

The structural trends discussed for NO<sub>2</sub> are also relevant for NO<sub>3</sub> adsorption. NO<sub>3</sub> is generally adsorbed in bridge configuration, where the N–O distance is elongated by ~0.04 Å with respect to the gas phase (from 1.24 to 1.28 Å). The increased N–O distance is similar to what is calculated for the gas-phase nitrate. Regarding the Ag<sub>n</sub> geometries, the tendency of cation structures is clearer than that for NO<sub>2</sub>. For Ag<sub>6</sub>NO<sub>3</sub>, the 2D and 3D structures are essentially degenerated. In the case of Ag<sub>7</sub>NO<sub>3</sub>, the 2D structure is preferred over the pentagonal pyramid by 0.11 eV. The difference between NO<sub>2</sub> and NO<sub>3</sub> correlates with the large difference in electronic affinity (EA). For NO<sub>2</sub>, the calculated adiabatic EA is 1.67 eV, whereas the corresponding value is 3.36 eV for NO<sub>3</sub>. Thus, it is reasonable that the tendency toward cation structures should be more pronounced for NO<sub>3</sub> adsorption.

The NO, NO<sub>2</sub>, and NO<sub>3</sub> adsorption energies are collected in Figure 3. NO<sub>3</sub> is clearly more strongly adsorbed than NO<sub>2</sub>, and NO has the lowest adsorption energy. Particularly for NO<sub>2</sub> and NO<sub>3</sub>, there is a pronounced odd/even alternation. In several cases, the adsorption energy changed in the order of 1 eV from one cluster size to another. Starting with the trimer, the marked changes correlate with differences in the ionization potential of the clusters. The changes in the adiabatic ionization potential (AIP) are calculated to be [AIP(Ag<sub>n</sub>) – AIP(Ag<sub>n-1</sub>)] –2.0, 0.7, –0.6, 0.8, –1.2, 0.6 eV for n = 3-8. For NO<sub>3</sub> adsorption on Ag<sub>3</sub> to Ag<sub>8</sub>, the differences in adsorption energies [ $E_a(Ag_n) - E_a(Ag_{n-1})$ ] are 3.1, –0.8, 0.7, –1.2, 1.0, and –0.7 eV, respectively.

2. Analysis of the Electronic Structure. The electronic structure of small  $Ag_n$  clusters have been analyzed previously.<sup>9</sup> States close to the HOMO level are of 5s character and are separated from the 4d electrons, which are well below the highest occupied states. The 5s-derived states are delocalized over the cluster. This results in a jellium nature of  $Ag_n$  clusters with clear electronic shell closings and a marked odd/even alternation in properties connected to the electronic structure.

Also for NO<sub>x</sub> adsorption, the properties of Ag<sub>n</sub> clusters are dominated by the 5s electrons. To analyze the bond in detail, the examples with NO and NO<sub>3</sub> on Ag<sub>4</sub> are considered. Ag<sub>4</sub> is chosen because the same cluster isomer is relevant for the bare cluster and the cluster with adsorbates. Because the nature of the NO<sub>2</sub> and NO<sub>3</sub> bond is similar, the discussion is restricted to the latter.

In Figure 4, the electronic density of states (EDOS) for Ag<sub>4</sub>, Ag<sub>4</sub>NO, and Ag<sub>4</sub>NO<sub>3</sub> are reported. For the bare cluster, the center of the d-derived states are localized at -7.5 eV. The spin-degenerated state at the upper edge of the d-band is the fully symmetric combination of 5s-derived states. The HOMO level is a 5s-derived state with a node at a symmetry plane. The LUMO<sup>46</sup> level is a similar type of state but with a perpendicular nodal plane. In the language of jellium clusters, the fully symmetric state corresponds to 1s, whereas the HOMO and LUMO are 1p states.

For Ag<sub>4</sub>NO, states mainly located at NO determine the character of the orbitals near the HOMO level. The HOMO level as well as the three first unoccupied states are of  $2\pi^*$  character. The molecular  $1\pi$  and  $5\sigma$  are centered at -12.2 and -11.4 eV,



**Figure 4.** Electronic density of states (DOS) for Ag<sub>4</sub> (left panel), Ag<sub>4</sub>-NO (middle panel), and Ag<sub>4</sub>NO<sub>3</sub> (right panel). The DOS is obtained by a 0.1-eV Gaussian broadening of the one-electron Kohn–Sham energies. Some selected Kohn–Sham orbitals are shown at an isosurface of  $\pm$  0.03 1/Å<sup>3</sup>.

respectively. The occupied metal states are hybridized with the NO orbitals in a minor fashion. The small effect of NO on the occupied orbitals correlates with the fairly weak interaction between NO and  $Ag_n$ .

NO<sub>3</sub> is found to have large effects on the electronic structure of Ag<sub>4</sub>. The 1s orbital is clearly affected by the adsorbates and polarized away from NO<sub>3</sub>. The state at -5.7 eV is mainly located at the adsorbate. In fact, this orbital corresponds to the HOMO level of NO<sub>3</sub>, which in the gas phase is singly occupied. However, in this case, the resonance has two electrons. This is another clear signature of nitrate formation, that is, transfer of one electron from the metal to the adsorbate. The HOMO level is now the singly occupied 1p state. The spin-down counterpart of this orbital is LUMO. The LUMO+1 state resembles the nature of another 1p state.

3. Vibrational Analysis. Vibrational infrared (IR) spectroscopy is a powerful technique that can be used *in situ* to probe the molecular species present in catalytic reactions. Because the mode of vibration is a signature of the potential energy surface experienced by the molecule, such measurements can reveal information on adsorption configuration and bond strengths.

In the present study, the method of finite differences was utilized to calculate the vibrational spectrum for NO, NO<sub>2</sub>, and NO<sub>3</sub> adsorbed on Ag<sub>n</sub>. For each cluster size, results for the stable adsorption configuration are reported in Figure 5. Although the complete spectra were evaluated, here the discussion is restricted to modes that correspond to internal adsorbate vibrations. The internal metal modes are below 200 cm<sup>-1</sup>.

In the gas-phase, the wavenumber of the NO stretch vibration is calculated to be 1932 cm<sup>-1</sup>. This is only a slight overestimation compared with the experimental value<sup>43</sup> of 1904 cm<sup>-1</sup>. The stretch vibration is clearly softened upon adsorption (lower panel of Figure 5). With the exception of Ag<sub>5</sub>, the NO stretch vibration is around 1700 cm<sup>-1</sup> for all investigated clusters. Just as for the adsorption energy, there is a slight odd—even alternation. The stretch vibration for NO adsorbed on even clusters are higher than that on the adjacent odd clusters. The low wavenumber (1545 cm<sup>-1</sup>) predicted for Ag<sub>5</sub> is owing to the bridging adsorption configuration for this cluster size. In this geometry, the HOMO of the cluster is efficiently interacting with the  $2\pi^*$ orbital of NO, which results in a low stretch vibration. It clearly



**Figure 5.** Calculated wavenumbers for NO, NO<sub>2</sub>, and NO<sub>3</sub> adsorbed on Ag<sub>n</sub>. The values to the left correspond to the calculated molecular gas-phase value.

correlates with the long intermolecular distance (1.21 Å) calculated for NO in this case.

The NO stretch vibration has been measured for neon matrixisolated AgNO<sup>47</sup> to be 1707 cm<sup>-1</sup>. This is in good agreement with the present result for AgNO of 1713 cm<sup>-1</sup>. In ref 21, the NO stretch vibration on Ag<sub>4</sub>NO was calculated to be 1873 cm<sup>-1</sup>, which is clearly higher than our result of 1719 cm<sup>-1</sup>. However, the vibrational shifts with respect to the gas-phase NO are comparable ( $\sim$ 200 cm<sup>-1</sup>). In ref 21, the vibration of gas-phase NO was reported to be 2076 cm<sup>-1</sup>.

For NO<sub>2</sub>, the wavenumbers for the asymmetric and symmetric stretch vibrations, together with the bend mode, are calculated to be 1710, 1390, and 760 cm<sup>-1</sup>, respectively. The corresponding experimental values<sup>48</sup> are 1618, 1318, and 750 cm<sup>-1</sup>. The cluster-size dependence of these modes are reported in the middle panel of Figure 5. The main character of the NO<sub>2</sub> LUMO level is a node between nitrogen and the two oxygen atoms in conjugation with an O-O bond. This character makes the asymmetric NO<sub>2</sub> stretch vibration sensitive to charging. Consequently, it is not surprising that the wavenumber corresponding to this mode is red-shifted by  $\sim 400 \text{ cm}^{-1}$  for NO<sub>2</sub> adsorbed on Ag<sub>n</sub> as compared to the gas-phase NO<sub>2</sub>. The symmetric vibration is also shifted to lower wavenumbers by  $\sim 200 \text{ cm}^{-1}$ . In agreement with the character of the NO<sub>2</sub> LUMO level, the bending mode is instead slightly shifted to higher energies by  $\sim 40 \text{ cm}^{-1}$ . The odd/even alternation present for the adsorption energies are also reflected in the vibrational signatures. In the gas phase, the bend and asymmetric stretch vibrations are IR active. Of the two modes, the asymmetric stretch is by far the most intense. When  $NO_2$  is adsorbed on  $Ag_n$ , the symmetric stretch vibration is also predicted to be IR active. Given the adsorption structure, this is not surprising. The intensities of the symmetric and asymmetric modes are calculated to be of similar strengths (~300 km/mol).

The NO<sub>3</sub> case is reported in the top panel of Figure 5. Three vibrational modes are reported, namely, the out of plane, the symmetric N–O stretch, and the asymmetric N–O stretch, of which the asymmetric stretch is doubly degenerated in the gasphase. The wavenumbers for these modes are calculated to be

780, 1110, and 1280 cm<sup>-1</sup>, respectively. The corresponding experimental values<sup>49</sup> are 762, 1060, and 1492 cm<sup>-1</sup>. As NO<sub>3</sub> is adsorbed, the degeneracy is broken for the asymmetric vibration. The two modes are separated by about 300 cm<sup>-1</sup> for all cluster sizes. The symmetric mode is softened upon adsorption by  $\sim 100 \text{ cm}^{-1}$ . Because the out of plane mode does not include motion in the direction toward the cluster, the wave number is calculated to be fairly unchanged upon adsorption. All of the vibrational modes show the same odd/even alternations as a function of cluster size as already discussed for NO and  $NO_2$ . The symmetric mode of  $NO_3$  in the gas-phase is not IR active. However, similar to the symmetric mode of NO<sub>2</sub>, it becomes active (~100 km/mol) as NO<sub>3</sub> is adsorbed on Ag<sub>n</sub>. The mode with the highest wavenumber of the two asymmetric vibrations is the most intense in the spectrum at  $\sim 600$  km/mol, whereas the asymmetric mode with the lowest wavenumber has an intensity of  $\sim 300$  km/mol.

## **IV.** Conclusions

Density functional theory was used to explore NO<sub>x</sub> adsorption on Ag<sub>n</sub> in the range from the monomer to the octamer. NO is found to interact weakly with Ag<sub>n</sub> and is preferably adsorbed in an atop configuration. In contrast, NO<sub>2</sub> and NO<sub>3</sub> are adsorbed in a bridge configuration. The adsorption energy between the molecules and the clusters follows the trend  $E_a(NO) < E_a(NO_2)$  $< E_a(NO_3)$ . Both NO<sub>2</sub> and NO<sub>3</sub> are bonded via charge transfer from the metal to the molecule. This charge transfer has a pronounced effect on the structure of the cluster. In general, isomers relevant for the cationic Ag<sub>n</sub> become energetically preferred. Marked odd/even effects dominate the size evolution of electronic properties of Ag<sub>n</sub> in the studied size regime. Consequently, odd/even alternations are present in adsorption energies as well as the evaluated vibrational spectra.

Recently, small silver clusters have been suggested to constitute the active phase in  $Ag/Al_2O_3$  catalysts for SCR with HC.<sup>12,13</sup> Given the large size variations in cluster properties, it will be important to investigate whether  $Ag_n$ , also supported, shows such marked size variations. One may speculate that either the support reduces the size variation or the functionality of the  $Ag/Al_2O_3$  catalyst is based on clusters with atomic resolution.

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